

# Adaptive Active Noise Control for Uncertain Secondary Pathes

Toshikazu Kouno, Hiromitsu Ohmori and Akira Sano

Department of System Design Engineering, Keio University,  
3-14-1 Hiyoshi, Kohoku-ku, Yokohama 223-8522, Japan

## Abstract

A new direct adaptive algorithm for feedforward active noise control (ANC) is proposed in a general case when the primary and secondary path responses are all uncertain. In order to reduce the actual canceling error, the two artificial errors are introduced and are forced into zero by adjusting three adaptive FIR filters in an on-line manner. The distinctive feature of the method is that the adjusted parameters do not have to converge to the true FIR parameters but some constants, then the reduction of the two errors can attain the canceling at the objective point. The effectiveness of the proposed algorithm is validated in experiments using an air duct.

## 1. Introduction

Active noise control (ANC) is a way of suppressing unwanted noises generated by the primary sound sources at objective positions by producing artificial secondary control sounds. Together with the development of high speed DSP, the ANC recently has found more and more applications in improving industrial and living environment [1]. In the aspect of control methodology, the adaptive feedforward control is a powerful tool in the ANC, since the path dynamics cannot be precisely obtained and may be uncertainly changing.

A variety of filtered-x adaptive algorithms have been proposed to attain improved canceling performance in the ANC [3][4][5]. We also presented a modified filtered-x adaptive algorithms using the extended error signal and proved the robust stability [6]. Almost all filtered-x approaches assume that the secondary path model is known a priori. Therefore, if the secondary path responses are unknown or uncertainly changeable, identification of the secondary path model is required and the filtered-x algorithms should be updated on a basis of the identified model, or the feedforward controller should also be re-designed in a real-time manner according to the identified path models [7]. However, the former approach is not stability-guaranteed and the latter scheme suffers from computational burden.

The aim of this paper is to propose a new direct adaptive control approach in which two modified errors are introduced and are forced into zero by adjusting three kinds of adaptive filters. The proposed method does not require explicit identification of the primary and secondary path dynamics, so the computational burden is improved compared to the indirect adaptive approach presented by the

authors [7]. Finally its effectiveness is validated in exper-

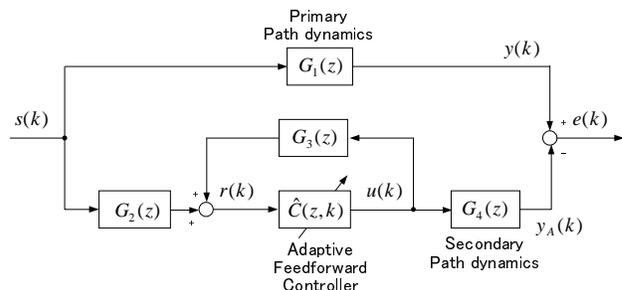


Figure 1: Schematic diagram of adaptive feedforward active noise control system

The schematic diagram of a single channel active noise control system is shown in Fig.1. The sound from the primary noise source is denoted by  $s(k)$  which is detected as  $r(k)$  by the reference microphone. The detected signal  $r(k)$  is used as the input to the adaptive feedforward controller  $\hat{C}(z, k)$ . The output of the controller  $u(k)$  is given to control the loudspeaker which emits the secondary artificial sound so that the noise at the objective point may be cancelled. The canceling error at the point is denoted by  $e(k)$ . All of the signals are characterized by four path dynamics, in which  $G_1(z)$  and  $G_2(z)$  represent the primary path dynamics, and  $G_3(z)$  and  $G_4(z)$  the secondary path dynamics, respectively, as given in Fig.1. Since all of the path dynamics may contain model uncertainty and parameter changeability, the adaptive control approaches are essentially important to deal with the problems. It follows from Fig.1 that

$$e(k) = G_1(z)s(k) - G_4(z)u(k) \quad (1)$$

$$u(k) = C(z)r(k) \quad (2)$$

$$r(k) = G_2(z)s(k) + G_3(z)v(k) \quad (3)$$

where  $C(z)$  be an FIR type of feedforward controller. Let  $\hat{C}(z, k)$  be an adaptive version of  $C(z)$ , then the secondary control sound is generated by

$$u(k) = \hat{C}(z, k)r(k) = \hat{\theta}^T(k)\varphi(k) \quad (4)$$

where  $\hat{\theta}(k) = [\hat{\theta}_1(k), \dots, \hat{\theta}_m(k)]^T$  and  $\varphi(k) = [r(k-1), \dots, r(k-m)]^T$ . Then the adaptive parameters to be

adjusted and the canceling error  $e(k)$  can be expressed from (1) ~ (4) as

$$e(k) = \bar{G}_1(z)r(k) - \bar{G}_4(z)u(k) \quad (5)$$

$$= \bar{G}_4(z) \left( \frac{\bar{G}_1(z)}{\bar{G}_4(z)} - \hat{C}(z, k) \right) r(k) \quad (6)$$

$$= \bar{G}_4(z)[(\theta^* - \hat{\theta}(k))^T \varphi(k)] \quad (7)$$

where  $\bar{G}_1(z) = G_1(z)/G_2(z)$  and  $\bar{G}_4(z) = G_4(z) + G_1(z)G_3(z)/G_2(z)$ . Thus it should be noted that the error system (7) for adaptation depends on all of the path dynamics.

## 2.2 Conventional Algorithms

### 1) Case with known secondary path dynamics

If the secondary path dynamics  $G_3(z)$  is known, the feedback effect by  $G_3(z)$  is cancelled by subtracting  $G_3(z)u(k)$  from  $r(k)$  to obtain  $G_3(z) = 0$ . As a result, it follows that  $\bar{G}_4(z) = G_4(z)$ , then we can realize the filtered-x algorithm if  $G_4(z)$  is also known, as

#### a) Filtered-x algorithms [3][5]

$$\hat{\theta}(k+1) = \hat{\theta}(k) + \mu\psi(k)e(k) \quad (8)$$

$$\psi(k) = G_4(z)\varphi(k) \quad (9)$$

where  $\mu > 0$  is a step size, and the normalized form is also used which is obtained by deviding the correction term in (8) by  $\rho + \psi(k)^T \psi(k)$ , ( $\rho > 0$ ).

#### b) Extended Error Based Filtered-x algorithm [6]

$$\hat{\theta}(k+1) = \hat{\theta}(k) + \gamma(k)\psi(k)\varepsilon(k) \quad (10)$$

$$\psi(k) = G_4(z)\varphi(k) \quad (11)$$

$$\varepsilon(k) = \frac{\eta(k)}{1 + \gamma(k)\psi^T(k)\psi(k)} \quad (12)$$

$$\eta(k) = e(k) + G_4(z)u(k) - \hat{\theta}^T(k)\psi(k) \quad (13)$$

where the extended error  $\varepsilon(k)$  defined by (12) and (13) is used instead of  $e(k)$ . The convergence and stability of the algorithm has been investigated by the authors [6].

### 2) Case with uncertain secondary path dynamics

A model of path dynamics includes uncertainties and actual dynamics will change due to temperature variations as in exhaust gas duct. When all the path dynamics are uncertain or changeable, the following on-line identification-based approach is essentially needed [7].

First, to identify the path dynamics  $\bar{G}_1(z)$  and  $\bar{G}_4(z)$  in (5) by using the accessible signals  $e(k)$ ,  $u(k)$  and  $r(k)$ , we adopt the identification models  $\hat{H}_1(z)$  and  $\hat{H}_4(z)$  as

$$\hat{e}(k) = \hat{H}_1(z)r(k) + \hat{H}_2(z)u(k) \quad (14)$$

The FIR coefficients in  $\hat{H}_1(z)$  and  $\hat{H}_2(z)$  can be updated by the LMS adaptive algorithm [7]. The dither signal modulated by the canceling error  $e(k)$  is needed in the explicit identification for achieving the PE condition.

Next, we compute the FIR adaptive feedforward controller  $\hat{C}(z, k)$  as  $\hat{C}(z, k) = \hat{H}_1(z)/\hat{H}_4(z)$ . This polynomial divisions can be executed by FFT and IFFT to obtain the stable  $\hat{C}(z, k)$  in real-time manner.

Thus, the various types of filtered-x adaptive algorithms need the reliable models for the secondary path dynamics. The above indirect adaptive approach is one of the solutions, but the computational burden of FFT and IFFT at every instant is rather high for real-time adaptation.

## 3. New Direct Fully Adaptive Algorithm

The conventional and extended-error based filtered-x algorithms require prior knowledge on the secondary path dynamics  $G_3(z)$  and  $G_4(z)$ . The aim of this paper is to propose a new direct adaptive algorithm which does not need explicit identification of the uncertain secondary path dynamics.

The basic structure of the proposed adaptive feedforward control algorithm is illustrated in Fig.2. It follows from the block diagram,  $e(k)$ ,  $e'(k)$  and  $e''(k)$  are computed as follows:

$$e(k) = \bar{G}_1(z)r(k) - \bar{G}_4(z)u(k) \quad (15)$$

$$e'(k) = e(k) + \hat{K}(z, k)u(k) - \hat{D}(z, k)r(k) \quad (16)$$

$$e''(k) = \hat{D}(z, k)r(k) - \hat{C}(z, k)x(k) \quad (17)$$

where  $\bar{G}_1(z)$  and  $\bar{G}_4(z)$  are defined in Section 2.1, and  $e'(k)$  and  $e''(k)$  are newly introduced as artificial errors for execution of the proposed direct adaptive algorithm. The control input  $u(k)$  and the auxiliary input  $x(k)$  are also defined as

$$u(k) = \hat{C}(z, k)r(k) \quad (18)$$

$$x(k) = \hat{K}(z, k)u(k) \quad (19)$$

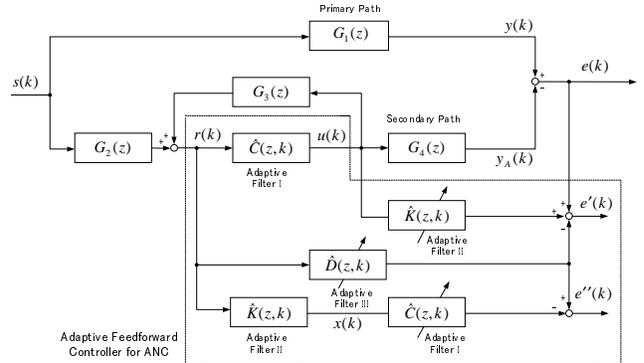


Figure 2: Direct adaptive algorithm for active noise control

It seems that  $\hat{D}(z, k)$  and  $\hat{K}(z, k)$  are the identified models for  $\bar{G}_1(z)$  and  $\bar{G}_4(z)$  respectively and the adaptive controller  $\hat{C}(z, k)$  is adjusted according to the identified models of the secondary path dynamics. However, the advantage of the proposed algorithm does not require the convergence of the adjusted parameters to their true



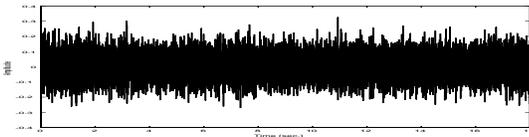


Figure 4:  $e(k)$  in case without control in Experiment 1

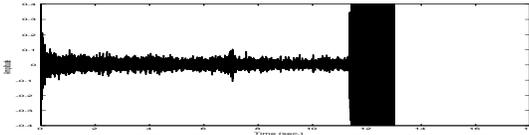


Figure 5:  $e(k)$  obtained by conventional filtered-x algorithm in Experiment 1

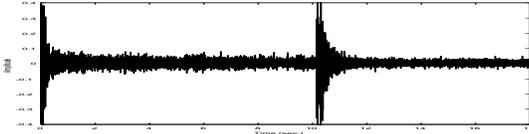


Figure 6:  $e(k)$  obtained by extended error based filtered-x algorithm in Experiment 1

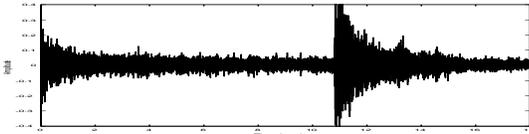


Figure 7:  $e(k)$  obtained by the direct fully adaptive algorithm in Experiment 1

before the experiment, and the obtained model was used in the algorithms (a) and (b) as the nominal model. At about 10 seconds after the start of control, the position of the reference microphone was switched from B' to B, which simulates uncertain changes in  $G_2(z)$  and  $G_3(z)$ . the Figs.4 to 7 show the time profiles of the error  $e(k)$  in cases with no control and  $e(k)$  in comparison with the three algorithms (a), (b) and (c). Since there is no changes in  $G_4(z)$  and very small changes in  $G_3(z)$ , the algorithms (b) and (c) could give very nice and stable performance (see Figs.6 and 7, respectively), but the algorithm (a) diverged because it is not stability-guaranteed even if  $G_4(z)$  is known (see Fig.5).

*Experiment 2:* The reference microphone was fixed at the position B, and the location of the error microphone was changed as A" → A → A' → A', that simulates uncertain changes of  $G_3(z)$  and  $G_4(z)$ . The step size of the all algorithm was chosen 2. The error  $e(k)$  is summarized in Figs.8 to 11. The algorithms (a) and (b) cannot be robust to the changes in  $G_3(z)$  and  $G_4(z)$  (see Figs.9 and 10 respectively), while the proposed direct adaptive algorithm (c) could give very stable performance to any changes in  $G_4(z)$  as shown in Fig.11.

## 5. Conclusion

We have presented the direct adaptive algorithm for updating the feedforward active noise controller, which will be applicable when the primary and secondary path

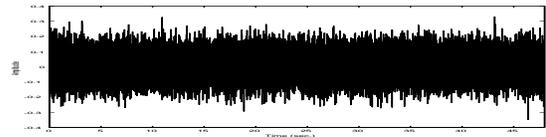


Figure 8:  $e(k)$  in case without control in Experiment 2

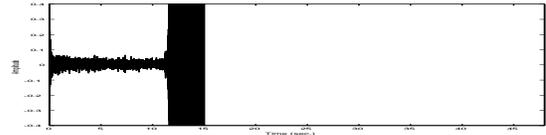


Figure 9:  $e(k)$  obtained by conventional filtered-x algorithm in Experiment 2

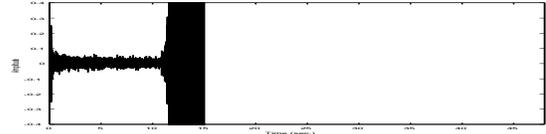


Figure 10:  $e(k)$  obtained by extended error based filtered-x LMS algorithm in Experiment 2

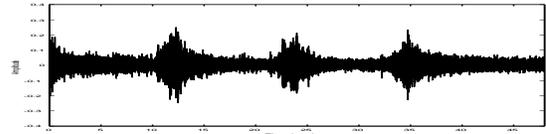


Figure 11:  $e(k)$  obtained by the direct fully adaptive algorithm in Experiment 2

dynamics are uncertain or unknown. The proposed algorithm involves three groups of adaptive filters updated so that the two artificial errors may be eliminated and then the actual canceling error can be cancelled.

## References

- [1] S. J. Elliot and P. A. Nelson: *Active Noise Control*, Academic Press, 1993.
- [2] D. R. Morgan, "An analysis of multiple correlation cancellation loops with a filter in the auxiliary path", *IEEE Trans. Acoust. Speech, and Signal Processing*, Vol. ASSP-28, pp.454-467, 1980.
- [3] L. J. Eriksson, "Development of the filtered-U algorithm for active noise control", *J. Acoust. Soc. Am.*, Vol. 89, pp.257-265, 1991.
- [4] E. Bjarnason, "Analysis of the filtered-x LMS algorithm", *IEEE Trans. Speech and Audio Processing*, Vol.3, No.3, pp.504-514, 1995.
- [5] S. M. Kuo and D. R. Morgan: *Active Noise Control Systems*, John Wiley and Sons, 1996.
- [6] F. Jiang, H. Tsuji, H. Ohmori and A. Sano, "Adaptation for active noise control", *IEEE Control Systems*, Vol.17, No.6, pp.36-47, 1997.
- [7] F. Jiang, H. Ohmori and A. Sano, "Identification-based multichannel adaptive active noise control with uncertain secondary channel dynamics", *Trans. IEEJ*, Vol. J78-A, No.2, pp.206-215, 2000.
- [8] V. Solo and X. Kong: *Adaptive Signal Processing Algorithms*, Prentice-Hall, 1995.